



SWAMI VIVEKANANDA SCHOOL OF

ENGINEERING & TECHNOLOGY

LECTURE NOTE

MACHINE DESIGN

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Machine Design

The subject machine design is the creation of new machines & improving the existing ones.

Classification of machine Design

① The machine design may be classified (i) Adaptive Design.
(ii) Development Design.
(iii) New Design.

ADAPTIVE Design

- (i) ADAPTIVE Design in which there is no need of special knowledge or skill.
- (ii) The designer only makes minor modification in the existing in the produce.

Development Design

- (i) Development Design the type of design which needs scientific training, skill, & design capability in order to modify the existing with a new idea.
- (ii) In this case the designer start from the existing design but the final produce quite different from the original one.

New Design

- (i) This type's of Design lost's on reach search technical ability, Creativity of thinking. In this case the Designer makes completely new produce.

General Consideration of machine Design.

- (i) Types of load & stress's cost by the load.

- (ii) motion of the part's of kinematic machine.
- (iii) Selection of material's.
- (iv) form & size of part's.
- (v) friction resistance & lubrication.
- (vi) Convenient & economical future's.
- (vii) use of standard part's.
- (viii) safety of operation.
- in workshop facility's.
- (ix) Number of machine to be manufacture.
- (x) Cost of construction. assembling

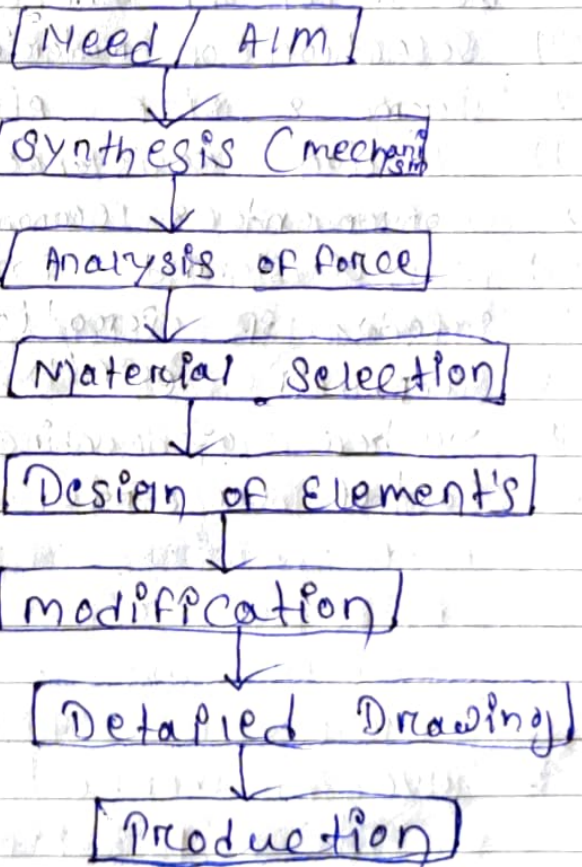
Important

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General Purpose Prossiger machine Design

In Designing of machine component There is no fixed role.

- ⇒ The problem may be shown in various ways but the General Prossiger to solve a Design Problem is as follows.

Recognition of Need

make a complete statement of the problem, indicating the need, Aim or Purpose for which the machine is to be Design.

Synthesis (mechanism) :

Select the possible mechanism or group of mechanism which give's the Desere motion.

Analysis of forces :

Find the forces acting in each member in machine & the energy transmitted by each member.

Material Selection :

Select the material which is best suitable for each member of machine.

Design of element's :

Find the size of each member of the machine by considering the force acting on the member's & the Permissible ^{stress} material used.

Modification :

modified the size of member to agree with past experience & judgment to facilitate manufacture.

(U) modification may also necessary by consideration of manufacturing to reduce overall cost.

Detailed Drawing

1) Draw the Detail Drawing of each component of the assemble / machine with complete specification.

Production

1) The component as per the drawing is manufacture on the work shop to make the machine.

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Engineering material & their
The knowledge of material & their properties are very important for an engineer during machine design.

(ii) Engineer broadly classified into broad

a) metal / alloys - Iron, steel, copper
b) non metal, brass.

non metal's : wood, sand, plastics
rubber, fibers

Again the metal's is classified in
2 groups

- (i) Ferrous metal's - (contain Iron%)
- (ii) Non-ferrous metal's (doesn't contain Iron percent)

Ferrous metal's - cast Iron, hot Iron,

Properties of the material's

(i) Physical Properties

The physical properties of metal include colour, size, mass, density, melting point, boiling point, electrical thermal conductivity etc.

Mechanical Properties

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Strength

It is the ability of a material to resist externally applied force without breaking.

Stiffness

It is the ability of a material to resist deformation.

Elasticity

It is the property of material to regain its original shape after deformation when the external forces are removed.

Plasticity

It is the property of material which retains the deformation produced by the load permanently.

Ductility

It is the property of a material enabling it to be drawn into wire with the application of a tensile force. In which we are able to draw into wire by the application of force. Ex: mild steel, Copper, aluminium, nickel, zinc, tin & lead.

Brittleness :

It is the property of a material opposite to ductility.

Ex - cast iron

Malleability $\frac{p}{a}$

It is a special case of ductility which permits/ allows materials to be rolled or hammered into thin sheets.

Ex - soft steel, wrought iron, copper & aluminium.

Touchness

It is the property of a material which refers to a relative ease with which a material can be cut.

Resilience

It is the property of a material to absorb energy & to resist shock & impact loads.

Workability

It is the property of material which refers to a relative ease with which material can be cut.

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Hardness

It is the properties of the material which resist to wear, scratch, deformation & machinability etc.

Creep

When a part is subjected to a constant stress at high temp for a long period of time. It will undergo a slow & permanent deformation called creep.

Fatigue Properties

When a material is subjected to repeated stress, it fails at a stress below the yield point stress. Such type of failure of a material is known as fatigue.

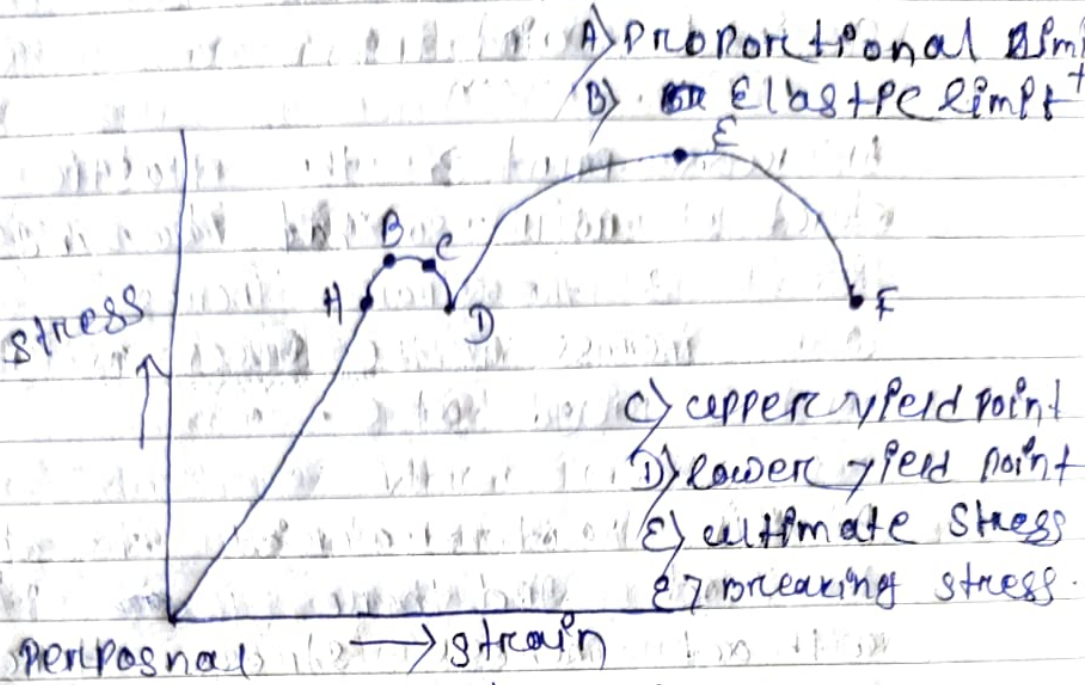
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Load

It is defined as any external force acting upon a machine part. A load may be 4 types

- (i) Dead or steady load
- (ii) Variable or variable load
- (iii) Suddenly applied or shock load.
- (iv) Impact load

Stress strain diagram (mild steel)



(i) When a mild steel is given to tensile stress, we find various points in the strain stress curve.

(ii) The various points are proportional limited. On the diagram from the point A to C, each a state line which represent that the stress is proportional to strain.

(iii) After point A, the curve suddenly change from the state line.

Elastic limit

It may be noted that even if the load is removed beyond point A or point B, the material will regain its size when the load is removed.

This means the material has elastic properties up to point B.

Yield Point

After the point B the plastic stage starts so that beyond the point B the strain increases faster with increase in the stress until the point is reached at C.

At this point material starts before the load and there is strain with an increase in stress. Hence there are two yield points, an upper yield point & lower yield point.

Ultimate Stress

At point D, the mild steel regains some strength and higher value of stress are required for higher strain.

The stress or load goes on increasing till the point E is reached. The gradual increase in strain of the mild steel is followed with the uniform reduction of its cross-sectional area. At point E the stress is which attains a value which is ultimate stress.

Breaking Stress

After the mild steel has reached ultimate stress, a neck is formed which is denser, the cross sectional area of the mild steel.

There fore the stress is reduce until the mild steel break away at point f. the stress comes ponding the point f is non of breaking stress.

Working Stress

when designing machine part it is desirable to keep the stress lower than the maximum or ultimate stress at which failure of the material take's place.

This stress is known as the working stress or design stress. It is also known as safe or allowable stress. by full over ~~the~~ not material ~~material~~ breaking of the material. Some machine part should be ~~then~~ when they have plastic deformation and they no more perform function.

Factor of Safety

It is defined as the ratio between maximum stress or working stress.

Factor of shafty = $\frac{\text{maximum stress}}{\text{Working stress}}$

* In case of ductility material, yield point clearly factor of shafty is base upon the yield point stress.

$$\text{Factor of shafty} = \frac{\text{Yield point stress}}{\text{Working stress}}$$

* In case of brittle material as iron, the yield point is not defined as for ductility material. ~~there~~ there force brittle the factor of shafty the brittle material base on

$$\text{Factor of shafty} = \frac{\text{ultimate stress}}{\text{Working stress}}$$

Definition of Factor of shafty

Stress in composite bar

A Composite Bar may be defined as a bar made off two or more material joint together in such a manner that the system extend contract as one unit when subjected to tension or compression.

1) The extension or contraction of a bar being equal to the strain

iii) The total external load on the bar is equal to the sum of the load carried by different materials.

Formula

$$P = P_1 + P_2$$

$$= \sigma_1 A_1 + \sigma_2 A_2$$

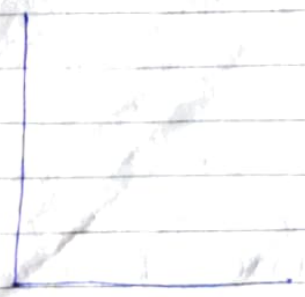
where P_1 or P_2 is load carried by bar one or bar 2.

σ_1 & σ_2 equal to stress produce by bar 1 or bar 2.

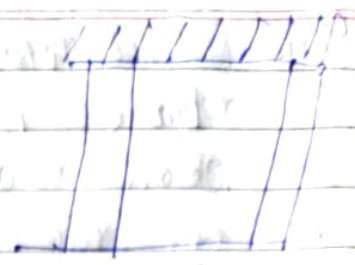
A_1 or A_2 = Cross sectional area of bar 1 & bar 2.

A bar 3 m long is made of 2 bars one of copper having $E = 105 \text{ GN/m}^2$ & other steel having E equal to 210 GN/m^2 each bar 25 mm broad & 12 mm thick this compound bar is stretch by a load 50 kN find the increase in length of the compound bar & the stress produce steel & copper. the length of copper as well as steel is 3 m.

Young's modulus (E) (C) = 105 GN/m^2
 thick ness = 12 mm
 $W = 50 \text{ kN}$



$L = 3 \text{ m} = 3 \times 10^3 \text{ mm}$
 $E_C = 105 \text{ GPa/m}^2$
 $E_S = 210 \text{ GPa/m}^2$
 $b = 25 \text{ mm}$
 $t = 12.5 \text{ mm}$
 $P = 50 \text{ kN}$



~~Area~~ The composite bar cross sectional area where area of the copper A_C = area of the steel A_S .

$$SE = AS \times Bt$$

$$B = 25 \times 12.5 = 312.5 \text{ mm}^2$$

Load share by the copper bar

$$P_C = P \times \frac{A_C \times E_C}{A_C \times E_C + A_S \times E_S}$$

$$= \frac{P \times E_C}{E_C + E_S}$$

$$= \frac{50 \times 105}{105 + 210}$$

$$= 16.67 \text{ kN}$$

Load share by steel bar

$$P_S = P - P_C = 50 - 16.67 = 33.33$$

Net elongation

$$\Delta l = \frac{P_C \times L}{A_C \times E_C} = \frac{P_S \times L}{A_S \times E_S}$$

$$= \frac{16.67 \times 3 \times 10^3}{312.5 \times 105}$$

$$= 1.52 \text{ mm}$$

(Ans)

We know that stress produced in the steel
 about 105 = ϵ_s by eq $\times 6 \text{ cm}$

$$= \frac{210}{105} \times 6 \text{ cm}$$

$$= 2 \text{ cm}$$

The total load $P = P_s + P_c = \epsilon_s \times A_s \times E_s + \epsilon_c \times A_c \times E_c$

$$P = \epsilon_s \left(\frac{P_s L}{A_c E_c} + \frac{P_s L}{A_s E_s} \right)$$

$$P_c = P_s \frac{A_c E_c}{A_s E_s}$$

$$P = P_c + P_s$$

$$P = \frac{P_s A_c E_c}{A_s E_s} + P_s$$

$$\Rightarrow P_s \left(\frac{A_c E_c}{A_s E_s} + 1 \right) = P$$

$$P_s = \left(\frac{A_c E_c + A_s E_s}{A_s E_s} \right) P$$

$$P_s = P \left(\frac{A_s E_s}{A_c E_c + A_s E_s} \right)$$

Thermal stress (stress due to change in temp)

When ever there is some increase or decrease in the temp of the body it causes the body will expand or contract a little. Consideration is so that if the body allow to expand & contract freely with the rise or fall of the temp ~~there~~ no stress are induce in a body.

But if the deformation of the body is prevented, some stress is induced in the body. Such stress is known as thermal stress.

$$\Delta L = L \alpha \Delta T$$

where ΔL = increase or decrease in length.

L = Rise or fall of temp in the body.

α = coefficient of thermal expansion.

If the end of the body is fixed to rigid support so that the expansion is prevented, then the compression strain is induced in the body.

$$\epsilon_c = \frac{\Delta L}{L} = \frac{L\alpha}{L} = \alpha T$$

Thermal stress

$$\sigma = \epsilon_c \times E = \alpha T E$$

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Working Stress
When design machine part, it is desirable keep the stress lower than the maximum or ultimate stress at which failure take place the stress is known as working stress. It is also called design stress, safe stress or allowable stress.

Factor of Safety

In General it is define the ratio of maximum stress to working stress.

Mathematical

$$F.O.S = \frac{\text{max}^n \text{ Stress}}{\text{working / safe stress}}$$

If the working stress of the machine is 200 KN/m^2 & the ultimate stress of the machine is 450 KN/m^2 what is the F.O.S the machine

working stress of the machine = 200 KN/m^2

& the ultimate stress = 450 KN/m^2

$$\text{The F.O.S} = \frac{\text{ultimate stress}}{\text{working stress}}$$

$$= \frac{450 \text{ KN/m}^2}{200 \text{ KN/m}^2}$$

$$= 2.25$$

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Design of Fastening Elements

Joint

Joint is the process in which we fix two or more than two similar or different material by temporary or permanent.

Types of Joint or Fastening

The fastening may be classified into two groups (1) permanent fastening (2) temporary

Permanent Fastening

The permanent are those fastening in which can't be separated without damaging the connecting material or components.

Ex - soldering, brazing, rebating, wetting etc.

Temporary Fastening

Temporary fastening those fastening can be separated without damaging the connected material or components.

Ex - nut & bolt, screw, key, splinds.

Welded Joint Process

welding - Joint is a process in which we fixed two or more than two similar or dissimilar materials by the application of heat with or without pressure.

Types of welding

welding process may be classified into two groups.

- (i) Fusion welding (with or without pressure)
- (ii) Forge welding (non-fusion) (with or without pressure)

Fusion welding

In fusion welding we only use heat.

- Types - Thermite welding
- Gas welding
- Electric arc welding etc.

Forge welding

In non-fusion welding we use both heat & pressure.

ex - Electric resistance welding

Types of welding joints

The welding joint may be 2 types

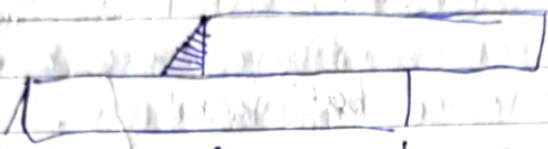
- (i) Lap joint
- (ii) Butt joint

Lap Joint

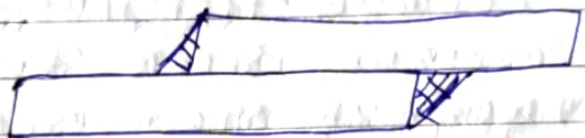
The lap joint the plate joint is often by overlapping the plates and then welding the edges the plates

Types

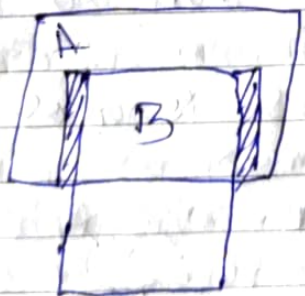
Lap joint may be single transverse lap joint (i) double transverse lap joint (ii) parallel lap joints



(single transverse)



(Double transverse fillet)



(Parallel fillet)


Built up Joints


The built joints is often by placing the plate's edge to edge in built welding the plate edges don't required bevelling if the thickness of the plate is less than 5mm. But than other hand if the plate thickness is 5 to 12.5 mm the edge should be


bevel to V or U groove in single or both sides.


Types

Square butt joint → 

single V butt joint → 

single U butt joint → 

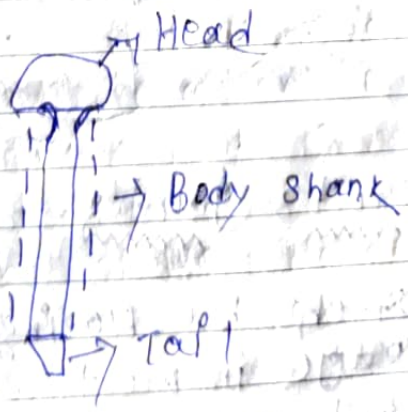
Double V butt joint → 

Double U butt joint → 

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Rebber Joint is the joint which is a permanent joint used to connect to or more than to materials by using rebber.

This process is known as Rebber Eng.



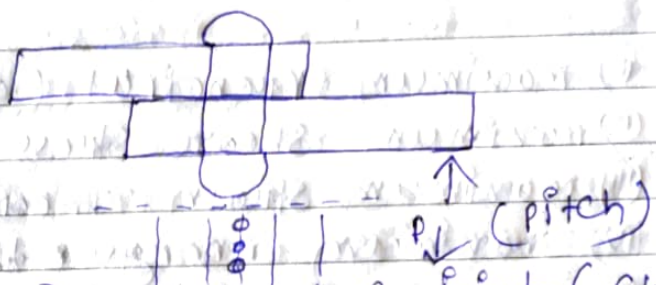
Type's of Riveted Joints

Basically the Riveted Joints divided into 2 groups \rightarrow Lap joint, Bolt joint

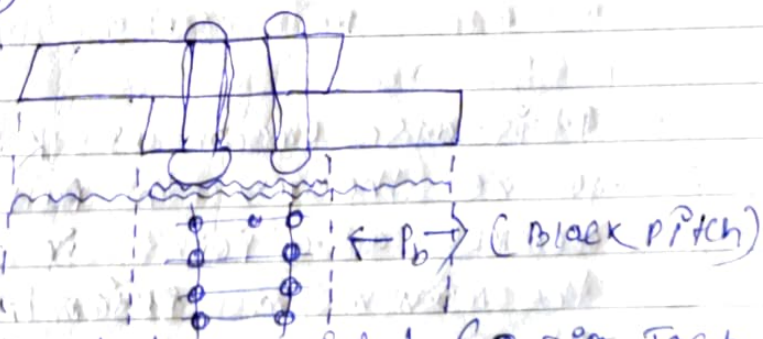
Lap Joint

A Lap joint is that in which one plate over lap of the other & the two plates are riveted together.

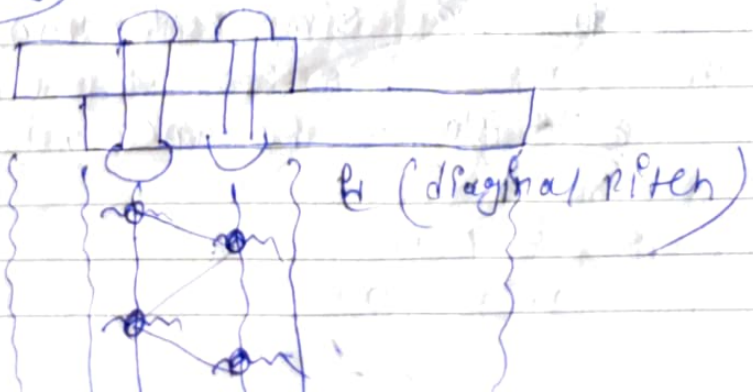
Single Riveted Lap joint



Double Riveted Lap joint (Chain Riveting)



Double Riveted Lap joint (Zig Zag Riveting)



Theory of Failure

11/10/2022

Theory of failure of the simple load the members are usually taken into account simple tension & compressive load. Theoretical failure prediction the failure of member is subjected uniform stress both simple state. Generalised the problem of predicting the failure stress of the members subjected to multiaxial or nonuniform stress is much more complicated.

(iii) The principal theory of failure of a member subjected to by axial stress are edge followers.

- (i) maximum principal (or normal) stress theory.
- (ii) maximum shear stress theory.
- (iii) maximum strain theory.
- (iv) maximum energy theory.
- (v) maximum distortion energy theory.

It is also known as Rankine's According to the theory the failure or yielding occurs at a point in a member when the maximum principal & normal stress of the by axial stress system equals strength of the material in the simple tension test.

Ex - Blash Furance,

maximum principal

(II) Maximum Shear stress theory

According to this theory failure or yielding occurs at a point in a member maximum shear stress in a 3D principal stress system reaches the value equal to the shear stress at yield point in a simple tension stress.

$$\tau_{max} = \frac{\sigma_y}{1.05}$$

τ_{max} - maximum shear stress
 σ_y = shear yield stress
 or 1.05 =

this failure mostly used for design of ductile material.

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(III) Maximum Principle Strain theory
Saint Venant

The other name is Saint Venant's theory.

According to this theory the failure or yielding occurs at a point in a member when the maximum principle or normal strain in a 3D principal stress system reach the limiting value of strain (that is strain at yield point) as determined in a simple tensile stress.

(11) The maximum tension in a normal stress
by a biaxial stress system.

$\epsilon_{max} =$ the maximum strain

$$\frac{\sigma_{11}}{E} = \frac{\sigma_{12}}{m \cdot E} = \frac{\sigma_{yt}}{E \cdot F.O.S}$$

MC - position ratio

$\epsilon_{max} =$ maximum shear strain

σ_{11} & σ_{12} = maximum & minimum by axial
stress system.

E = Young's modulus.

F.O.S = factor of safety.

This theory is not used in general
because it's early given reliable in
plastic cases.

maximum strain energy theorem :

which theorem

According to this theorem the failure
or yielding occurs at a point in a
member when the strain per unit volume
in any axial stress system reaches the strain
energy. (that is i.e.) strain energy
in a yield point per unit volume of
simple tensile stress.

(12)

The strain energy

maximum strain energy theorem

$$U = \frac{1}{2} \left[(\sigma_{t1})^2 + (\sigma_{t2})^2 - 2\sigma_{t1} \times \sigma_{t2} \right]$$

This theory may be ductile material.

maximum destruction theory / Hencky von Mises theory

According to this theory, the failure or yield occurs in a point of the member when the destruction strain energy per unit volume in a biaxial stress system reaches the limiting per unit volume in a uniaxial simple tensile test.

(ii) The maximum destruction theory the yield is expressed

$$(\sigma_{t1})^2 + (\sigma_{t2})^2 - 2\sigma_{t1} \times \sigma_{t2} = (\sigma_y)^2$$

It is applicable to ductile material. It is shear strain energy theory.

Resilience

When a body is loaded with in elastic limit it changes its dimension & on the removal load it regain the original dimension.

(i) At long age it regain. loaded it has so foric energy it said. on the removing load the energy store is given of is the stress of spring.

(ii) It is energy in observed the body when strained. or elastic limited is known as strain energy.

(iii) the strain energy is always applicable for some one.

✓ Strain energy store in a body due to external body, within elastic limit is known as resilience.

✓ The maximum energy which can be store for a body, elastic limit is called proof resilience.

modulus of resilience

The proof resilience per unit volume of a material is called modulus of resilience.

$$\text{mathematically} = \frac{\sigma^2}{2E}$$

σ - tensile / compressive stress

E - young's modulus

Different mechanical materials / 10/22

Cast Iron

Primarily an alloy of iron and carbon. Composition of cast iron is 2 to 4% carbon and 0.1 to 0.3% silicon. Cast iron is brittle material, can't you in mass of machinery which are subject to cast.

low cost good casting high compressive strength, wear resistance & the excellent machinery.

Compressive strength of cast iron is more of cast iron.

Types of Cast Iron

- (1) Grey cast iron
- (2) white cast iron
- (3) chilled cast iron
- (4) mottled
- (5) malleable cast iron.

Grey cast iron

The composition grey cast iron 2 to 3.5% carbon, silicon 1 to 2.75% manganese 0.10 to 1.0%, P 0.15 to 1%, sulphur 0.02 to 0.15% the rest are iron.

Grey color due to carbon are present free graphite.

* These materials are used low tensile strength strength or high compressive strength. No ductility - due to free graphite they are use lubricant (sliding motion & desire) machine tool body. Automatic cylinder block heads houses fly wheel, press & pipe fitting.

White Cast Iron

Composition of white cast iron Carbon 1.75-2.2%, Silicon 0.85 to 1.2% Mg less than 0.4%, P less than 0.2% Sulphur less than 0.12% & the remaining part the iron.

Have a high tensile strain & low compressive strain not use in machine with ordinary cutting tool but require grinding & a shapping machine.

Chill cast iron

After pouring white cast iron chill iron use in any face of a casting which are require have to with stand & wire friction.

Mottled cast iron

Produce between grey or white cast iron, composition colour grey & use in casting where strength.

malleable cast iron

This cast iron which solidified in the condition of graphite pieces structure total carbon content is present in it's combine form of cementite.

- (i) It is ductile it is bend without breaking of portion of section.
- (ii) tensile strain good & have excellent machining quality.
- (iii) use of the steel forging could be expanded.
- (iv) use hubs of small fitting for various rolling shock, break supports parts of agree culture carcinoma, pipe fitting, ~~Handing~~ English, locks

Alloys cast iron

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- (i) some amount of silicon, mg, P, phosphorus and also have nickel, chromium, copper, molybdenum.
- (ii) more strength & result in improve profit.
- (iii) increasing strength high wear resistance, corrosion resistance & heat resistance.
- (iv) used in alloys cast iron in gears, automobile, pipe, cylinder, piston, piston rings, crank, crankshaft, wheel, pulley, break, break drum, shoes & part off crushing & the grinding machining.

Composition of Pig Iron

- (i) Pig Iron
 - Carbon 2.5%
 - Silicon 0.12%
 - Sulphur 0.01%
 - Phosphorus 0.02%
 - Manganese 0.05%

(ii) Production of Mottled Iron by Puddling Process

- (i) It has a property of mottledness, mainly due to the use of iron forging or rolling.
- (ii) It is used for the chains, chain hook, rivets, boiler, steam pipe, water.

Steel

Steel is alloys of iron or carbon. Carbon 1.5%, some amount of silicon, P, S, Mn.

Type of Steel

- (i) Dead mild steel of to 0.15%
- (ii) Low carbon or mild steel 0.15% to 0.45%
- (iii) Medium carbon steel 0.45 to 0.8%
- (iv) High carbon steel 0.8% to 1.5%

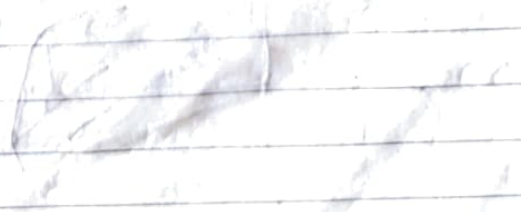
Free Cutting Steel

Free Cutting Steel has sulphur & phosphorus. Carbon 0.1 to 0.7%, Sulphur 0.05 to 0.2%, Lead 0.05 to 0.2%.

Alloys Steel
Steel with more amount of carbon, Alloys is done for special purposes like increasing wire resistance, corrosion resistance & to improve the electrical & magnetic properties.
use in steel are nickel, chromium, cobalt, silicon, molybdenum, tungsten.

Hook's Law

within elastic limit
 $\sigma \propto \epsilon$



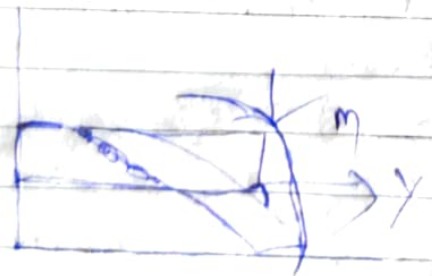
Models of Failures

- (i) A starting load ~~reach~~^{is} a force which gradually applied to a mechanical component of system which does not change with magnitude & direction with respect to time.
- (ii) engineering materials are classified into 2 groups - ductility, brittleness.
- (iii) The ductility material that is aluminium, structural steel, one have a relatively high tensile strength before fracture takes place.
- (iv) other hand, A Brittle material that cast iron has a relatively low tensile strain before fracture.

Three mode of failures

- (i) ~~material~~ failure's by electric deflection
- (ii) failure by General yielding
- (iii) failure by factor of safety

Failure of electric deflection



in application like transmission shafts supporting gears the maximum force acting in the shafts without effecting

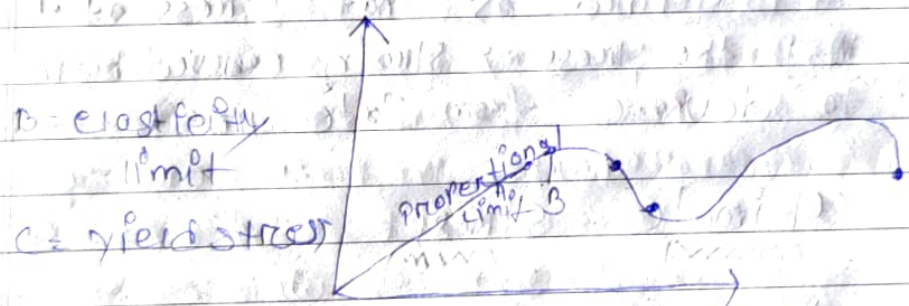
is performance limited by the permanent (plastic) elastic deformation.

(ii) Distortion or dimensional stability is considered as the criterion of design in such cases.

(i) Failure by "General Yielding"

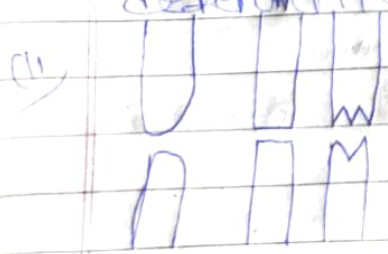
(i) ~~For~~ the mechanical component made of ductility material loses its engineering usefulness due to a "large amount of plastic deformation" after the yield point stress is reached.

(ii) Considerable portion of the of the component is subjected to plastic deformation to called General Yielding.

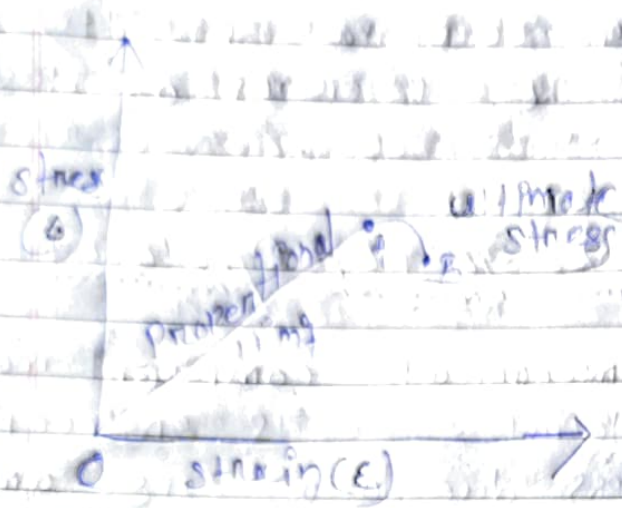


(ii) Failure by fracture

Component made of brittle material function satisfactory because of the sudden fracture with out plastic deformation.



Stress & strain diagram of cast iron



Proportional limit

OA express Hooke's law i.e. it is known as proportional limit.

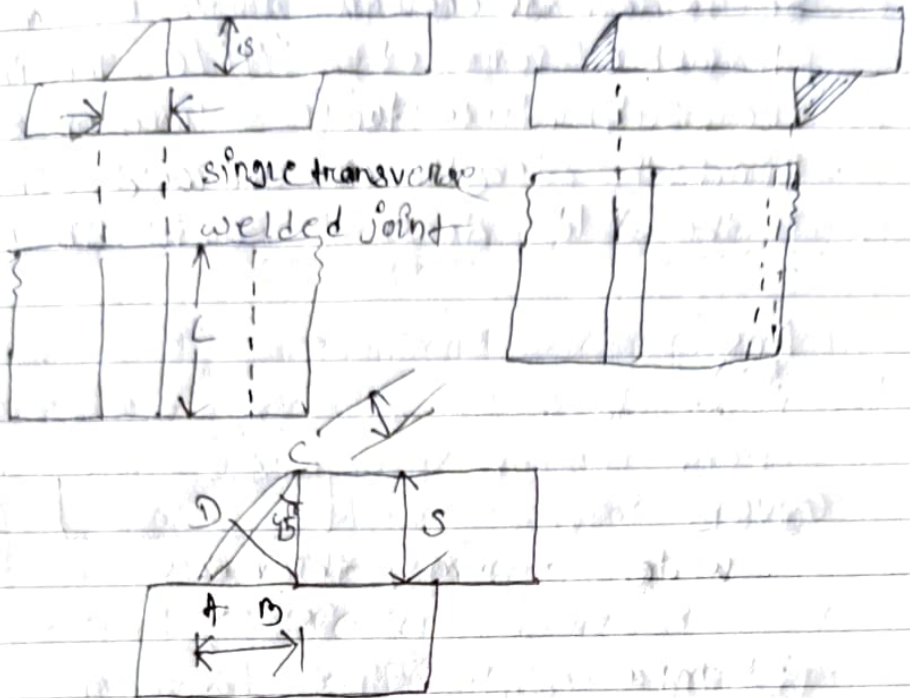
It is defined as that stress at which the stress & strain curve begins to deviate from straight line.

Ultimate stress

At B the specimen requires some stress of higher value or stress one required for higher strain than those between A & B.

18/10/2022

Strength of Transverse Joint / Lap Joint Welding



Let T = throat thickness edge welding to the perpendicular length of high Potanous

~~The perpendicular~~ ^{high Potanous} length of Edge welding to the perpendicular length of high Potanous.

Edge size of weld

The throat thickness (t) = $s \times \sin 45^\circ$

$$\text{Area of weld} = L \times T$$

$$= L \times 0.707s$$

σ_t = tensile stress

external force (P)

$$P = \sigma_t \times L \times 0.707s$$

for double transverse welding $P = 2 \times$

$$2 \times \sigma_t \times L \times 0.707s$$

20, 10, 22

①

A plate 100 mm wide & 10 mm thick is to be welded to another plate by means of double parallel fillet the plate are subject to static load of 80 kN. Find the length of the weld, shear stress in the weld doesn't exceed 55 MPa.

Ans

Given

width = 100 mm, thickness

55 MPa

21, 10, 22

② A plate 100 mm wide & 12 mm thick is to be welded to another plate by means of parallel fillet. The plate are subject to static load of 50 kN. Find the length of weld, shear stress in the weld doesn't exceed 50 MPa.

First under static loading on both plates

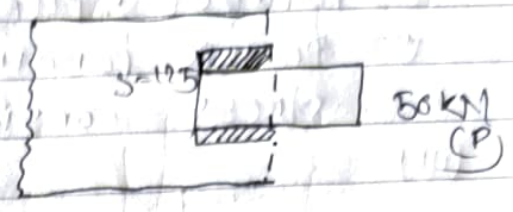
Given data

width = 100 mm

thick = 12.5 mm

load (P) = 50 kN = $50 \times 10^3 \text{ N}$ $\sigma_{\text{max}} = 56 \text{ MPa}$ F 55 N/mm²

nanometer meter	micro meter	milli meter	centi meter	deci meter	meter	hecto meter	kilo meter	mega meter
--------------------	----------------	----------------	----------------	---------------	-------	----------------	---------------	---------------



$$P = 6 \text{ mm} \times 2 \times 0.707 \times 8 \times L$$

$$50 \times 10^3 = 55 \times 2 \times 0.707 \times 12.5 \times L$$

$$\Rightarrow L = \frac{50 \times 10^3}{55 \times 2 \times 0.707 \times 12.5}$$

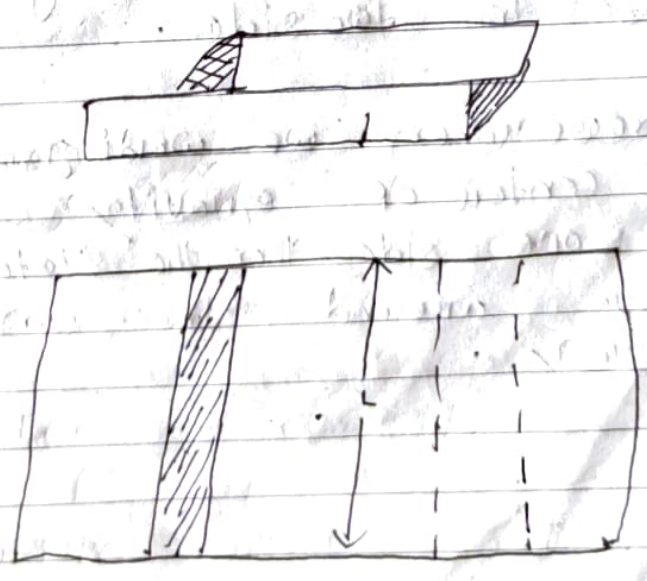
effective length = 501 mm
 length = 51 + 12.5 = 63.5

Transverse fillet weld

When the applied force is perpendicular to the length of the weld is called transverse fillet weld.

(i) In this fillet weld consider the simple stress

(ii)



~~Transverse~~ fillet weld

(i) When the applied force is parallel to the length is the weld is called parallel fillet weld

(ii) In this parallel fillet joint shear stress consider.

(iii)



In the static load stress ~~conside~~ concentration factor is one that means stress

$$\text{Effective Stress} = \frac{\text{stress}}{\text{concentration factor}}$$

fatigue load stress ~~conside~~ concentration factor is 2.7 that means effective stress = stress

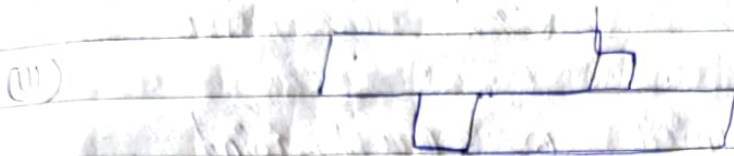
combination of single transverse and parallel welding

Why parallel fillet welding are occur in two side.

because when we welding in 1 side the center of gravity is change in the one side then the plate are remove around the center of gravity.

Lap joint

- (i) In the lap joint the plane of the welding of the two plate is called angle is 90° is called lap joint.
- (ii) A plate is overlapping the other plate.

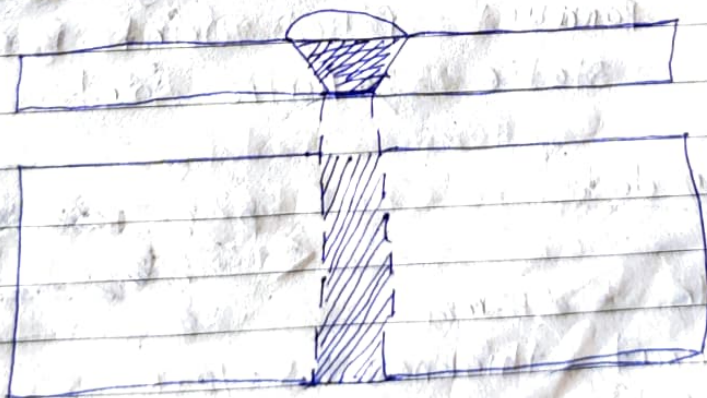


Bolt joint

- (i) The plane of plate's of bolt joint is same.
- (ii) In bolt joint two side of the plate are welding.



Strength of the bolt joint



Single V-bolt joint

(1) In Butt joint the size of weld (s) = throat or thickness (t) (t)



Load carried by butt joint

$P = \text{Area} \times \text{stress}$

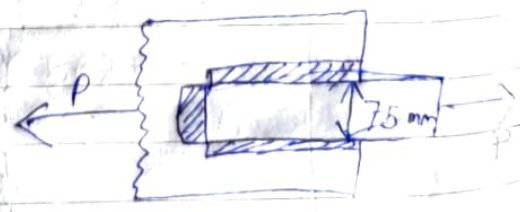
$= t \times L \times \sigma_t / 2$

$P = \text{Area} \times \text{stress}$

$= (t_1 + t_2) \times L \times \sigma_s / 2$

A plate 75 mm wide & 12.5 mm thick is joining in the another plate single transverse joint & double parallel joint as shown in figure the maximum tensile & shear stress 70 MPa & 56 MPa respectively. find the length of the each parallel plate joint is subject both static & cyclic joint

Given data



width = 75 mm

throat thickness = $s = 12.5$

$\sigma_t = 70 \text{ MPa} = 70 \text{ N/mm}^2$

$\tau = 56 \text{ MPa} = 56 \text{ N/mm}^2$

effective length of transverse weld
 $75 \text{ mm} = 12.5 \text{ m}$
 62.5 mm

Let

L_1 = length of the Transverse weld
 L_2 = length of the parallel fillet weld

Length of the each parallel starting load
 Now total load applied the plate
 $P = \text{Area} \times \text{Stress}$

$$= 75 \times 12.5 \times 70$$

$$= 65625 \text{ N}$$

Load of transverse weld

$$P_1 = \text{Area} \times \text{Stress}$$

$$= L_1 \times t \times 70$$

$$= 62.5 \times 12.5 \times 70$$

$$= 54687.5 \text{ N}$$

Load of parallel fillet weld

$$P_2 = \text{Area} \times \text{Stress}$$

$$= 2 \times L_2 \times t \times 56$$

$$= 2 \times L_2 \times 12.5 \times 56$$

$$= 1400 L_2$$

$$P = P_1 + P_2$$

$$65625 \text{ N} = 54687.5 + 1400 L_2$$

$P_1 = \text{Load applied to the transverse case}$
 $\text{Stress} \times \text{Area of weld}$
 $= 56 \times C_1 \times 0.7078$
 $= 70 \times 62.5 \times 0.707 \times 12.5$
 $= 38664.06 \approx 38664 \text{ N}$

P_2 = load applied to the parallel fillet weld.

$$\text{Total load } (P) = P_1 + P_2$$

$$= 65625 - 38665$$

$$= 9910$$

length of weld for static load

Effective stress of transverse weld

$$= \frac{6t}{1.5} = \frac{70}{1.5} = 46.66 \approx 47 \text{ N/mm}^2$$

Effective stress on parallel weld

$$= \frac{Z}{2.7} = \frac{56}{2.7} = 20.74 \approx 21 \text{ N/mm}^2$$

P_1 = load applied to transverse

= stress \times Area

$$= 47 \times 62.5 \times 0.707 \times 12.5$$

$$= 25960 \approx 25960$$

P_2 = load applied to parallel weld

= stress \times Area

$$= 21 \times 2 \times 0.707 S \times L_2$$

$$= 21 \times 2 \times 0.707 \times 12.5 \times L_2$$

$$= 371.175 L_2$$

Total load $P = P_1 + P_2$

$$L_2 = \frac{65625 - 25960}{371}$$

$$L_2 = 160.97 \approx 167 \text{ mm}$$

effective length parallel weld

$$= 107 + 12.5 = 119.5 \text{ mm}$$

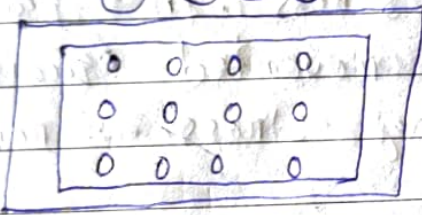
$$= 120 \text{ mm}$$

Based on ^{no} of rivet on plate rivet:



single lap Riveted joint

single butt Riveted joint



Strap Butt Double Riveted joint

Terminology

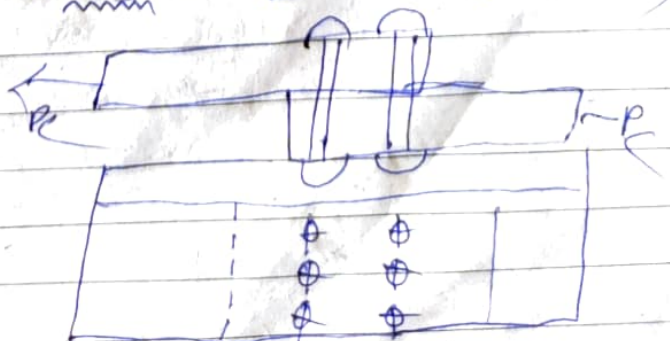
W = width of plate

P =

d = diameter of rivet

$$d = 0.75 \sqrt{P}$$

Compressive stress \rightarrow (Crushing stress)



$$P_c = \text{Stress} \times \text{Area}$$

$$= \sigma_c \times n \times d \times t$$

$$= \sigma_c \times n \times d \times t$$

q.1, q.2, q.3 10.1, 10.4, 10.5, 10.6

02/11/2022

Q-
mm

Find the efficiency of the following riveted joint.

A single riveted lap joint of 6 mm plates with 20 mm diameter rivets having a pitch of 50 mm.

ii) Double riveted lap joint of 6 mm plates with 20 mm diameter rivets having a pitch of 65 mm. Assume permissible tensile stress in plate 120 mpa, permissible in rivets equal to 90 mpa, permissible crushing stress in rivets 180 mpa.

Given data

Single riveted lap joint

$$t = 6 \text{ mm}$$

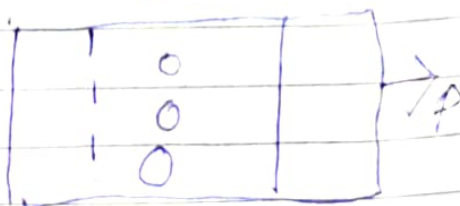
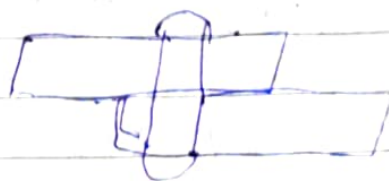
$$d = 20 \text{ mm}$$

$$p = 50 \text{ mm}$$

$$\sigma_t = 120 \text{ mpa} = 120 \text{ N/mm}^2$$

$$\sigma_c = 90 \text{ mpa} = 90 \text{ N/mm}^2$$

$$\sigma_{cr} = 180 \text{ mpa} = 180 \text{ N/mm}^2$$



In case of tensile load

$$\begin{aligned} P &= \text{Stress} \times \text{Area} \\ &= 120 \times (\pi \times d) \times t \\ &= 120 \times (\pi \times 50) \times 6 \\ &= 113097.34 \text{ N} \end{aligned}$$

In case of shear stress

$$\begin{aligned} P_s &= 2 \times n \times \frac{\pi}{4} d^2 \\ &= 90 \times \pi \times \frac{\pi}{4} \times (20)^2 \\ &= 28274 \text{ N} \end{aligned}$$

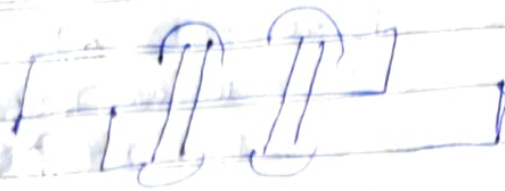
In case of compressive stress

$$\begin{aligned} P_c &= \sigma_c \times \pi \times d \times t \\ &= 180 \times \pi \times 20 \times 6 \\ &= 21600 \text{ N} \end{aligned}$$

$\eta = \frac{\text{Strength of riveted joint of plate}}{\text{Strength of an riveted joint of plate}}$

$$\begin{aligned} &= \frac{21600}{113097.34} \\ &= 0.191 \end{aligned}$$

$$\begin{aligned} \text{Efficiency} &= 0.191 \times 100 \\ &= 19.1\% \quad (\text{Ans}) \end{aligned}$$



	0	0	
	1	0	
	1	0	

Given data

$$P = 65 \text{ mm}$$

$$d = 20 \text{ mm}$$

$$t = 6 \text{ mm}$$

$$\sigma_t = 120 \text{ mpa} = 120 \text{ N/m}^2$$

$$\sigma_c = 90 \text{ mpa} = 90 \text{ N/m}^2$$

$$\sigma_c = 180 \text{ mpa} = 180 \text{ N/m}^2$$

in case on tensile load

$$P_t = \sigma_t \times (P-d) \times t$$

$$= 120 \times (65-20) \times 6$$

$$= 32400 \text{ N}$$

in case of shear load

P

Strength of the riveted joint

$$P = P \times d \times t$$

$$= 69 \times 100 \times 120$$

$$= 96800 \text{ N}$$

Efficiency = $\frac{\text{strength of riveted or plate joint}}{\text{strength of un-riveted or plate joint}}$

$$= \frac{32400}{96800} = 69\%$$

$$\therefore 69 \times 100 = 69\% \text{ An}$$

A double riveted double cover butt joint in plate 20mm thick is made with 25mm diameter rivets. The permissible stresses are: tensile = 120 mpa, 100 mpa, 150 mpa. Find the efficiency of joint taking the strength of the riveted in double age twice than the single shear given data

$$t = 20 \text{ mm}, P = 100$$

$$d = 25 \text{ mm}$$

$$\sigma_t = 120 \text{ mpa} = 120 \text{ N/m}^2$$

$$\sigma_s = 100 \text{ mpa} = 100 \text{ N/m}^2$$

$$\sigma_c = 150 \text{ mpa} = 150 \text{ N/m}^2$$

tensile load

$$P_t = \sigma_t \times (P-d) \times t$$

$$= 120 \times (100-25) \times 20$$

$$= 180000 \text{ N}$$

shear stress =

$$P_s = \sigma_s \times 2 \times \pi \times \frac{3}{4} d^2$$

$$= 100 \times 2 \times \pi \times \frac{3}{4} \times 25^2$$

$$= 196349 \text{ N}$$

Compressive stress

$$\begin{aligned}
 & \sigma_c \times r \times d \times T \\
 & = 1500 \times 20 \times 0.5 \times 0.0 \\
 & = 15000
 \end{aligned}$$

efficiency = $\frac{\text{strength of riveted joint}}{\text{strength of an unriveted plate}}$

$$\eta = \frac{15000}{120 \times 100 \times t} = 0.625 \times 100$$

$\eta = 62.5\%$ (Ans)

Date: 04/11/2022

Design of boiler joint.

A boiler has a longitudinal joint as well as circumference joint.

The longitudinal joint is used to joint the end of the plate to get the required diameter of the boiler.

ii) The circumference joint is used to get required the length boiler.

Longitudinal joint of a boiler.

$$t = \frac{PD}{2\sigma + \eta c} + 1 \text{ (corrosion allowance)}$$

S. S. S. S.

P = steam pressure / gauge pressure in boiler

D = internal diameter of boiler shell

S_t = permissible stress

η_c = ~~vertical~~ efficiency of longitudinal

Note

The thickness of the boiler shell should not be less than 7 mm

If the thickness of the boiler shell is less than 7

2) Diameter of Riveted Boiler:

If $t \geq 8\text{mm}$

$d = 6\sqrt{t}$

If $t < 8$

$t = p_c$

Margin - $15d$

3) Pitch of the rivets

$P = Ct + M$

Distance between

$P_b = 0.33P + 0.67d$
($21g \geq P$)

$P_b = 2d \rightarrow$ Chain

Thickness of the Bolt Joint

$$t_1 = 1.125 t \quad (\text{single cover})$$

$$t_1 = 0.625 t$$

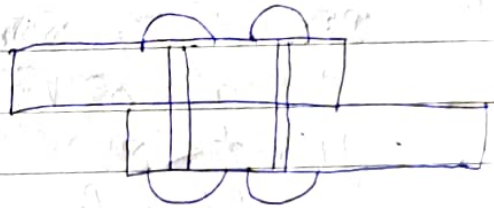
$$t_1 = 1.125 t \cdot \left(\frac{p-d}{p-2d} \right) \quad (\text{single cover alternating rivets})$$

$$t_1 = 0.625 t \cdot \frac{p-d}{p-2d}$$

$$t_1 = 0.75 t \quad (\text{inside boiler})$$

05/11/22

Ex - A Double riveted lap joint with zig zag Riveted Design for is to be Design for 15 mm thick plate. Assume $\sigma_t = 80 \text{ mpa}$, $\sigma_s = 60 \text{ mpa}$, $\sigma_c = 120 \text{ mpa}$. state how the joint will fail & find the efficiency of joint.



0	0	
1	0	
1	0	

$$t = 13 \text{ mm}$$

$$\sigma_t = 80 \text{ mpa} = 80 \text{ N/mm}^2$$

$$\sigma_s = 60 \text{ mpa} = 60 \text{ N/mm}^2$$

$$\sigma_c = 120 \text{ mpa} = 120 \text{ N/mm}^2$$

(1) thickness of Bolt

Diameter of rivet
 $d_1 = 22 \text{ mm}$

3) Pitch of the rivet's

$$P_{\max} = C_t + 4d$$

$$= 0.62 \times 13 + 41$$

$$= 75.06 \text{ mm}$$

$$P_t = (P - d) \times t \times 6t$$

$$= (P - 23) \times 13 \times 80$$

$$P_s = (n \times R_s) \times \frac{\pi}{4} \times d^2 \times Z$$

$$= (n \times 2) \times \frac{\pi}{4} \times (23)^2 \times 6$$

$$= (n \times 2) \times 2492$$

$$= 49857 \text{ N}$$

$$P_t = P_s$$

$$\cancel{(P - 23)} \times 13 \times 80 = 49857$$

$$\Rightarrow (P - 23) = \frac{49857}{13 \times 80}$$

$$P = 47.88 + 23 = 71$$

Pitch of rivet = 71 mm

4) Distance b/w rows of rivet

$$P_b = 0.33P + 0.67d$$

$$= 0.33 \times 71 + 0.67 \times 23$$

$$= 38.84$$

$$= 39 \text{ mm}$$

5

margine

$$m = 1.5d$$

$$= 15 \times 23$$

$$= 345 \text{ mm}$$

$$P_t = (p-d) \times t \times G_t$$

$$= (71 - 23) \times 13 \times 80$$

$$= 49920 \text{ N}$$

$$P_s = (nR) \times \frac{\pi}{4} \times d^2 \times Z$$

$$= 2 \times \frac{\pi}{4} \times 23^2 \times 60$$

$$= 49857 \text{ N}$$

$$P_c = (n \cdot n) \times (d \times t) G_c$$

$$= 2 \times 23 \times 13 \times 120$$

$$= 71760$$

Q) Efficiency of riveted joint

$$\eta = \frac{\text{least of } P_t / P_s / P_c}{P \times t \times G_t}$$

$$= \frac{49857}{71 \times 13 \times 80}$$

$$= 0.9$$

0.4, 0.5, 0.6, 0.7, 0.8, 0.9

Q. 7. Design a Double riveted butt joint with 2 covered plates for a longitudinal seam of a boiler shell 1.5 m diameter subjected to a steam pressure 0.95 N/mm^2 . Assume joint efficiency $\eta = 75\%$ allowable tensile stress in the plate 90 megapascals compressive stress 140 mpa & shear stress in the riveted 56 mpa .

Given data

$$D = 15, = 1500 \text{ mm}$$

$$P = 0.95 \text{ N/mm}^2$$

$$\eta = 75\% = 0.75$$

$$\sigma_t = 90 \text{ mpa} = 90 \text{ N/mm}^2$$

$$140 \text{ N/mm}^2$$

Given data

thickness of plate :

$$t = \frac{PD}{2\sigma_t \eta} + 1$$

$$= \frac{0.95 \times 1500}{2 \times 90 \times 0.75} + 1$$

$$= 11.5/12 \text{ mm}$$

$$= 11.5/12 \text{ mm}$$

Diameter of the riveted

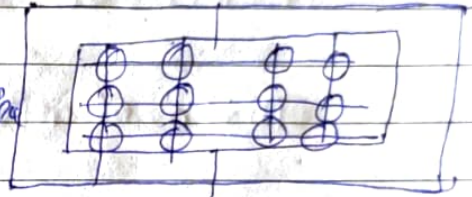
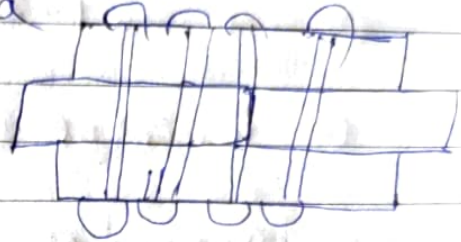
$$= 6.05 \sqrt{t} = 21$$

$$= 6.05 \sqrt{12} = 20.98/21 \text{ mm}$$

$$\text{Pitch} = (P-d) + X \cdot d$$

$$= (P-21) \times 12 \times 90$$

$$= (P-21) \times 1080 \text{ N}$$



Shearing strength of riveted

$$= P_s = (n \times r) \times \phi \times 2 \times d^2 \times Z$$

$$= (n \times 2) \times \phi \times (21)^2 \times 0.6$$

$$P = \frac{38792}{400000} \quad \text{--- (2)}$$

Eq (1) or (2) Part

$$P = 21 \times \frac{38792}{1080}$$

$$P = \frac{38792}{1080} + 21$$

$$= 56.91 \text{ mm}$$

$$= 57 \text{ mm}$$

Pitch of riveted 57 mm (Ans)

Distance between rows of rivet (P_b)

$$= 0.33p + 0.67d$$

$$= 0.33 \times 57 + 0.67 \times 21$$

$$= 32.88 = 33 \text{ mm (Ans)}$$

Assume Chain drive

$$P_b = 2d$$

$$= 2 \times 21$$

$$= 42 \text{ mm (Ans)}$$

5) thickness of shaft

$$t_1 = 0.625 d$$

$$= 0.625 \times 12$$

$$= 7.5 \text{ mm (Ans)}$$

margin = $1.5 \times d$

$$= 1.5 \times 21$$

$$= 31.5 \text{ (Ans)}$$

The load on the joint

3rd CHAPTER

Shafts and keys

11/11/2021

Moment of shaft = Force x Perpendicular distance (N/mm)

Moment of Inertia

Ob - Bending Stress (N/mm²)

12/11/22

shaft is a rotational machine element which is used to transmit power one place to another.

Function of shaft

(i) The power is deliver to the shafted by some tangential force & resultant force. Hence (Twisting) moment set of with in the shafted transmit the power to the transfer to various machine link of shaft.

(ii) In order to transfer the power shaft to another the various member such as a pulley gear etc are mounted on it.

(iii) These members anole with the forces exerted on them of cause the shaft to bending.

(10) In other word, we may say that a shafted is used for the transmission of torque on bending moment.

(11) The various members are mounted on the shafted by means the key & springs

material used for the shafted

- (i) It should be high strain.
- (ii) It should good machine ability.
- (iii) It should have low notch sensitivity.
- (iv) It should be good heat treatment property.
- (v) It should be high wear resistance property.
- (vi) The material use for the shaft have in this property is necessary.

Type's of shaft

They are 2 type of shaft used in design

- (i) ~~TP~~ Transmission.
- (ii) machine shaft & rigid shaft

Transmission shaft

These shaft transmit power between the source & the machines absorbing power

The counter shaft, line shaft or over head shaft & old factor shaft are transmission shaft. Since these shaft carry machine ~~shaft part~~ such as pulley gear etc. therefore they are subjected to

bending in addition to twisting.
 (ii) These shafts form internal part of the machine part like crank shaft, cam shaft & the cam of the machine shaft.

Design of shaft ϕ

① Consider twisting moment / Torque -

$$\frac{T}{J} = \frac{Z}{R} = \frac{C \cdot \theta}{\phi}$$

$$= \frac{T}{J} = \frac{Z}{R}$$

$$= \frac{T \times R}{J}$$

$$= T \times \frac{d}{\frac{\pi \times d^3}{32}}$$

$$\frac{T}{J} = \frac{Z}{R}$$

$$= \pi = \frac{2 \times J}{T}$$

$$\Rightarrow \frac{d}{2} = \frac{2 \times \frac{\pi \times d^3}{32} \times d^2}{T}$$

$$= d = \frac{2 \times 2 \times \pi \times d^3}{32 \times T}$$

$$d = \frac{2 \times \pi \times d^3}{16 \times T} \Rightarrow d = \frac{2 \times \pi \times d^3}{16 \times T}$$

15, 11, 22

Page No. _____

Date: / / 20

- ① consider the torsion
- ② and the bending stress
- ③ combination of torsion and bending

Max. hollow

$$\frac{d_o}{2} = \frac{\tau}{32} \times \frac{\pi (d_o^4 - d_i^4)}{T} \times 2$$

$$d_o = \frac{\tau \times \pi (d_o^4 - d_i^4) \times 2}{32 \times T}$$

$$d_o \Rightarrow \frac{\tau \times \pi (d_o^4 - d_i^4) \times 2}{16 \times T}$$

$$\tau = \frac{\tau}{32} \times d_o^4 - d_i^4$$

$$P = \frac{2\pi \times N \times T}{60}$$

A line shaft rotating at 100 RPM is to transmit 20 kW. The shaft may be assumed to be made of mild steel. Allowable shear stress is 42 MPa. Determine the shaft diameter neglecting the bending moment on the shaft.

Given data

$$N = 100 \text{ rpm}$$

$$P = 20 \text{ kW} = 20 \times 10^3$$

$$T = \frac{20 \times 10^3 \times 60}{2 \times \pi \times 100}$$

$$= 1909.85$$

$$= 1910 \text{ Nm-mm}$$

$$d = \sqrt[3]{\frac{16 \times T}{\pi \times \tau}} = \sqrt[3]{\frac{16 \times 1910}{\pi \times 42}} = 6.14 = 6 \text{ mm}$$

16/10/22

Find the diameter of solid shaft to transmit 20 kW at 200 rpm. The ultimate shear stress of the steel may be taken 360 MPa and the factor of safety is 8. If hollow shaft is to be used in place of the solid shaft find the ratio of the diameter when the ratio of inside or outside diameter D_1 .

Given data:

$$P = 20 \text{ kW} = 20 \times 10^3 \text{ W}$$

$$N = 200 \text{ RPM}$$

$$\text{ultimate shear stress} = 360 \text{ MPa}$$

$$\text{solution } = 360 \text{ N/mm}^2$$

allowable shear stress

$$Z = \frac{\text{ultimate stress}}{\text{F.O.S}}$$

$$= Z = \frac{360}{8} = 45 \text{ N/mm}^2$$

$$= 45$$

$$\text{Power (P)} = \frac{2\pi N T}{60}$$

$$20 \times 10^3 = \frac{2 \times \pi \times 200 \times T}{60}$$

$$T = \frac{20 \times 10^3 \times 60}{2 \times \pi \times 200}$$

$$= 954.92 \text{ say } 955 \text{ N}\cdot\text{mm}$$

Solid shaft

Diameter of shaft

$$= d = \sqrt[3]{\frac{16 T}{\pi \times 45}} = 9.76 \text{ mm}$$

$$= 5 \text{ mm}$$

For hollow cylinder shaft

$$d_o = \sqrt[3]{\frac{16 \times 1965}{\pi \times 95 \times \{1 - (0.5)^4\}}}$$

$$= 4.86 \approx 5 \text{ mm}$$

$$d_i = k \times d_o$$

$$= 0.5 \times 5$$

$$= 2.5 \text{ mm}$$

2) Shaft subjected to bending.

$$\Rightarrow \frac{M}{I} = \frac{\sigma_b}{y} = \frac{E}{R}$$

$$\Rightarrow \frac{M}{I} = \frac{\sigma_b}{y}$$

$$\Rightarrow \frac{I}{M} = \frac{y}{\sigma_b}$$

$$\Rightarrow \frac{\frac{\pi}{64} \times d^4}{M} = \frac{d}{2 \times \sigma_b} \Rightarrow \frac{\pi \times d^4}{64 \times M} = \frac{d}{2 \times \sigma_b} \Rightarrow \frac{\pi \times d^3}{32 \times M} = \frac{1}{\sigma_b}$$

$$\Rightarrow d = \sqrt[3]{\frac{32 \times M}{\pi \times \sigma_b}} = \left(\frac{32 \times M}{\pi \times \sigma_b} \right)^{1/3}$$

For hollow shaft

$$= \frac{M}{\frac{\pi}{64} \times (d_o^4 - d_i^4)} = \frac{\sigma_b}{\frac{d_o}{2}}$$

$$M = \frac{\sigma_b \times 2}{d_o} \times \frac{\pi}{64} \times (d_o^4 - d_i^4)$$

$$= \frac{\sigma_b \times \pi}{32} \times \left(\frac{d_o^4 - d_i^4}{d_o} \right)$$

$$M = \frac{\pi \times \sigma_b}{32} \times \frac{d_o^4}{d_o} \left\{ 1 - \left(\frac{d_i}{d_o} \right)^4 \right\}$$

$$M = \frac{\pi \times \sigma_b}{32} \times d_o^3 \times (1 - k^4)$$

$$d_0 = \sqrt[3]{\frac{32 \times 10^6}{2 \times 10^6 \times (1.5)^2}}$$

14.4

A pair of wheels of a rail wagon carrying a load of 50 kN on each wheel. Acting at a distance 100 mm outside the wheel base. The gauge of the rail is 1.5 m. Find the distance of rails between the wheels if the stress is not to exceed 100 MPa.

Given data

$$F = 50 \text{ kN} = 50 \times 10^3 \text{ N}$$

$$L = 10 \text{ m} = 1.0 \times 10^3 \text{ mm}$$

$$E_b = 100 \text{ MPa} = 100 \times 10^6 \text{ N/mm}^2$$

$$m = \text{force} \times \perp \text{ distance}$$

$$= 50 \times 10^3 \times 100$$

$$= 5 \times 10^6 \text{ Nmm}$$

$$d = \sqrt[3]{\frac{32 \times 5 \times 10^6}{2 \times 10^6}}$$

$$= \frac{79.85 \text{ say}}{80} \text{ (Ans)}$$

17/11/22

Shaft subjected both torsion & Bending

maximum shear stress

$$\tau_{max} = \frac{1}{2} \sqrt{(G\theta)^2 + (4Z)^2}$$

due to torsion

maximum normal stress

$$\sigma_b_{max} = \frac{1}{2} \sigma_b + \frac{1}{2} \sqrt{(G\theta)^2 + 4Z^2}$$

Bending moment

$$\frac{M}{I} = \frac{G\theta}{r}$$

$$\Rightarrow G\theta = \frac{M \times r}{I}$$

$$\Rightarrow G\theta = \frac{M \times \frac{d}{2}}{\frac{\pi}{64} d^4}$$

$$\Rightarrow G\theta = \frac{M \times d \times 64 \times 32}{\pi \times d^4 \times 2} \Rightarrow G\theta = \frac{M \times 32}{\pi \times d^3}$$

Torsion equation

Torsion equation

$$\frac{T}{J} = \frac{\tau}{r}$$

$$= z = \frac{T \times r}{J}$$

$$= z = \frac{T \times \frac{d}{2}}{\frac{\pi}{32} d^4}$$

$$= z = \frac{16T}{\pi \times d^3}$$

FE

$$Z_{\max} = \frac{1}{2} (6b)^2 + 4zR$$

$$= \frac{1}{2} \times \left[\left(\frac{32m}{\text{std } 3} \right)^2 + \left(4 \times \frac{16T}{\text{std } 3} \right) \right]$$

$Z_{\max} \Rightarrow$

$$(6b)_{\max} = \frac{1}{2} 6b + \sqrt{\frac{1}{2} (6b)^2 + 4zR}$$

$$= \frac{1}{2} \times \frac{32}{\text{std } 3} + \sqrt{\frac{1}{2} \left(\frac{32m}{\text{std } 3} \right) + 4 \left(\frac{16T}{\text{std } 3} \right)}$$

$$= \frac{16m}{\text{std } 3} + \frac{16}{\text{std } 3} \sqrt{m^2 + T^2}$$

$$(6b)_{\max} = \frac{16}{\text{std } 3} \left[m + \sqrt{m^2 + T^2} \right]$$

A shaft made of mild steel is required to transmit 100 kW at 300 rpm. The supported length of the shaft is 3 m. It carries two pulleys each exerting 1500 N. supported at a distance of 1 m from the end respectively. Assuming the safe value of stress.

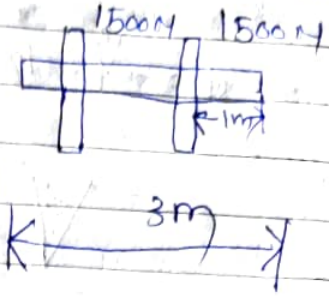
Given data

$N = 300 \text{ rpm}$

$P = 100 \text{ kW} = 100 \times 10^3 \text{ W}$

$\omega = 1500 \text{ N}$

$L = 3 \text{ m} = 3 \times 10^3 \text{ mm}$



We know that

$$P = \frac{2\pi NT}{60}$$

$$\Rightarrow 100 \times 10^3 = \frac{2\pi \times 300 \times T}{60}$$

$$= \frac{100 \times 10^3 \times 60}{2\pi \times 300}$$

$$= 3183.09 \text{ N-mm}$$

Maximum Bending moment at C/D

$$m = 1500 \times 100 = 15 \times 10^5 \text{ Nmm}$$

Equivalent Torque

$$\sqrt{\frac{\pi}{16} \times d^3 \times Z} = \sqrt{m^2 + T^2} \quad \text{--- formula}$$

Assume $Z = 60 \text{ N/mm}^2$

$$\frac{\pi}{16} \times d^3 \times 60 = \sqrt{m^2 + T^2}$$

$$= \frac{\pi}{16} \times d^3 \times 60 = \sqrt{(15 \times 10^5)^2 + (3183)^2}$$

$$= \sqrt{(15 \times 10^5 \text{ mm})^2 + (3183 \times 10^3)^2}$$

$$= 3518.7 \times 10^3 \text{ Nmm}$$

$$= 351.87 \times 10^3 \text{ N/mm}$$

$$d = \sqrt[3]{\frac{15 \times 10^5 \times 10}{\pi \times 60}}$$

$$= 66.87 \text{ say } 67 \text{ (Ans)}$$

19,

240 RPM, determine the diameter of the shaft if the maximum torque transmitted exceed a mean torque by 20% take the maximum available shear stress $\tau = 60 \text{ MPa}$.

Given data

$$P = 1 \text{ MW} = 1 \times 10^6 \text{ W}$$

$$N = 240 \text{ R.P.M}$$

$$T_{\text{max}} = 20\% T_{\text{mean}}$$

$$= \frac{20}{100} \times T_{\text{mean}}$$

$$= 0.2 \times T_{\text{mean}}$$

$$\tau = 60 \text{ MPa} = 60 \text{ N/mm}^2$$

We know that

$$P = \frac{2\pi N T}{60} \Rightarrow T_{\text{mean}} = \frac{P \times 60}{2\pi N}$$

$$\Rightarrow \frac{1 \times 10^6 \times 60}{2\pi \times 240} \Rightarrow 39788.73 \text{ N}\cdot\text{m}$$

$$\Rightarrow 39788.73 \times 10^3 \text{ N}\cdot\text{mm}^2$$

T_{max}

$$= 0.2 \times 3978872 \times 10^3$$

$$= 7957746$$

$$d = \sqrt[3]{\frac{16T}{\pi \tau}}$$

$$= \sqrt[3]{\frac{16 \times 7957746}{\pi \times 60}} = 87.74$$

$$= 87.74 \text{ mm (Ans)}$$

21, 11, 2022

Key's

A key is a piece of mild steel inserted between the shaft & hub on Boss or a Pulley to connect them together in order to prevent relative motion between them.

It is always inserted parallel to the axis of the shaft.

Function of key

Key's are used to temporarily fastening & subjected to considerable crushing & shearing stress.

↳ The key way is a slot cut in shaft & hub of the Pulley to accommodate a key.

Types of key

The following types of key are important.

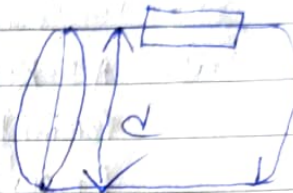
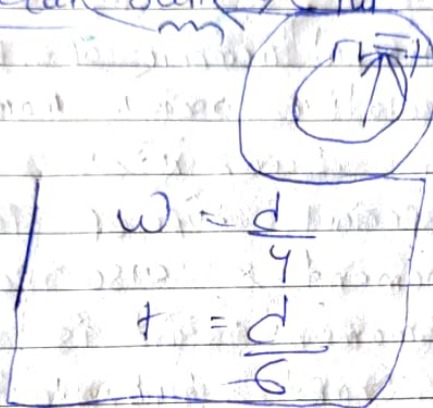
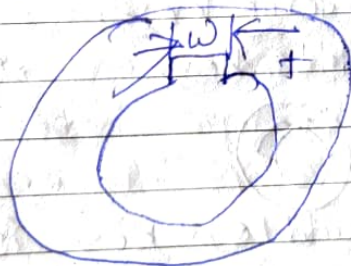
- (1) Sunk key
- (2) Saddle key
- (3) Taper key
- (4) Tangent key
- (5) Round key
- (6) Splines

Note

In shearing stress the key are failure in case of crushing stress the shaft.

Sunk Key

- (1) Rectangular Sunk Key
 - (2) Square Sunk Key
 - (3) Parallel Sunk Key
 - (4) Gib-head Sunk Key
 - (5) Feather Sunk Key
- 1) Rectangular Sunk Key

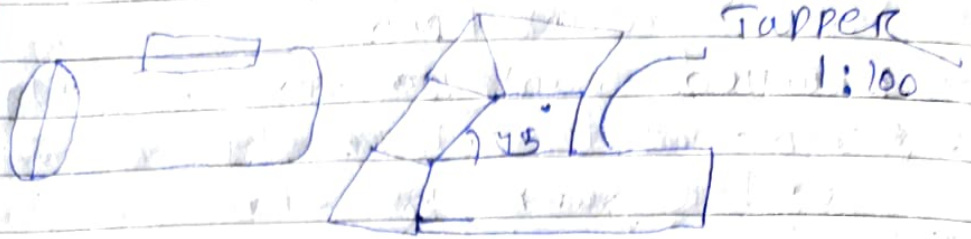
2) Square Sunk Key

$$w = t = \frac{d}{4}$$

Parallel sunk key may be of rectangular & square section uniform in width & thickness through out.

It may be noted that A Parallel taperless key is used where the pump gear or other mating piece is required to slide along the shaft's.

Gib head sunk key



Q. A key attached member of any pair & which permit relative axial movement is non-axial fastened "Sunk key"

Q. It is special type of parallel key a tapering moment & also permit also axial movement. It is fastened either to the shaft & hub, to the key being a sliding feed in the key way of the moving piece.

22/11/22

Types of saddle key
Flate saddle key



A flate saddle key is a taper key which is fit in a key way in the hole and is flate on the shaft.

It is likely to slip round the shaft under load. therefore it is used to comparatively light load.

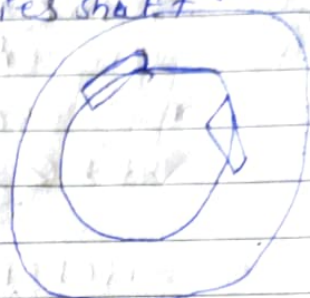
Hole saddle key

is a taper key which fits in a key way on the hub and the bottom of the

key have 2 feet the curved surface:

Tangent Key

A Tangent key are the fitted in pair in acute angle. is key to with stand torsion in one direction only. these are used large heavy duties shaft.



Round Key

A Round key, are circular & across section & fit into hollow drilled partly in the shaft & partly in the hub.



Spines

key's are made integral with the shaft which feet in the on the hub such shaft is known as splined shaft.



$$D = 1.125d$$

$$to \le 0.25 \phi$$

Design of key

torque = force distance

$$= C \times L \times \frac{t}{2} \times \frac{d}{2}$$

$$2 \times w \times l \times \frac{t_c}{2} = \frac{6C_{17}}{2}$$

$$\Rightarrow \frac{2w}{t} = \frac{6C}{Z}$$

$$\Rightarrow \frac{w}{t} = \frac{3C}{Z}$$

$$\frac{I}{t} = \frac{3C}{Z} = C_0$$

$$I = \frac{2 \times J}{R} = \frac{2 \times J \times d^3}{32}$$

$$\frac{2 \times J \times d^3}{32 \times d} = \frac{2 \times J \times d^3}{16}$$

Design a Rectangular Key for a Shaft of 50mm dia. The Shearing & Crushing Stress for the key material are 42 mpa, 70 mpa.

Rectangular key

Given data

$$d = 50 \text{ mm}$$

$$\tau = 42 \text{ mpa} = 42 \text{ N/mm}^2$$

$$\sigma_c = 70 \text{ mpa} = 70 \text{ N/mm}^2$$

Rectangular key

$$w = 16$$

$$t = 10$$

$$\text{Shearing Strength (Ps)} = w \times L \times \tau$$

$$= 16 \times L \times 42$$

$$= 672 L$$

$$\text{Shearing Torque} = \frac{Ps \times d}{2}$$

$$= 672 \times 25$$

$$= 1680 \text{ L N-m}$$

$$T = \frac{\tau}{R} \times J \Rightarrow 2 \times 2 \times d^3 \times \frac{1}{32} = 2 \times 2 \times 3$$

$$= 42 \times \frac{\tau \times (50)^3}{16} = 1030835 \text{ L. say}$$

$$16800 \text{ L} = 1030835$$

$$L = \frac{1030835}{16800} = 61.35 \approx 61 \text{ mm}$$

$$\text{Crushing strength (Ps)} = \frac{L}{2} \times 52 = 1675 \times 52 = 86000 \text{ N} \cdot \text{cm} \times 5 \times 70 = 350$$

$$\text{Crushing Torque} = 350 \times \frac{d}{2} = 350 \times 25 = 8750 \text{ L. Nm}$$

$$8750 \text{ L} = 1030835$$

$$L = \frac{1030835}{8750}$$

$$= 117.80 \text{ mm} = 118 \text{ mm}$$

Effect of key ways

$$K = 1 + 0.2 \left(\frac{w}{d} \right) + 1 \cdot 1 \left(\frac{h}{d} \right)$$

e = error factor shaft strength factor
 w

(i) A little consideration that the key ways curved of shaft, load carrying capacity of the shaft.

(ii) This is due to stress consideration near the corner key way & the reduction cross section of the shaft.